

## Unit 24, Session 3.

In all sciences, when we model data describing physical phenomena, we should always be aware of the units the values have.

When we use functions in our models like  $\sin(\ )$ ,  $\cos(\ )$ ,  $e^{(\ )}$ ,  $\ln(\ )$ , we will want to remember that what ends up in the  $(\ )$  doesn't have units.

In modeling RC decay, we found that the potential difference across the discharging capacitor, as a function of time, is given by

$$\Delta V_C = \Delta V_0 e^{(-t/RC)}$$

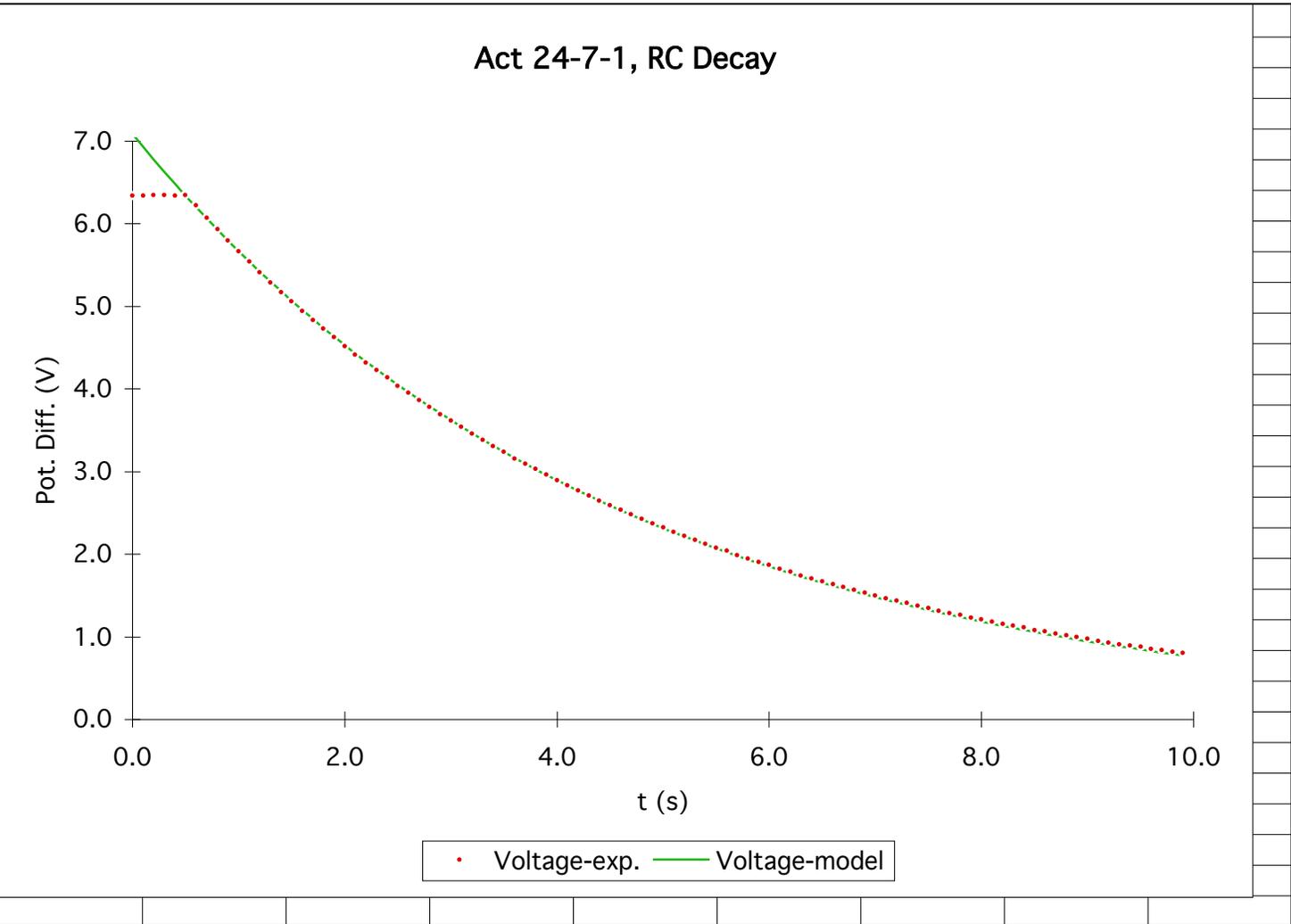
$t$  is in seconds, and since  $(t/RC)$  doesn't have units, the product  $RC$  must also be in seconds:  $[\Omega] [F] = [s]$

We use this information to characterize and compare different  $RC$  circuits.

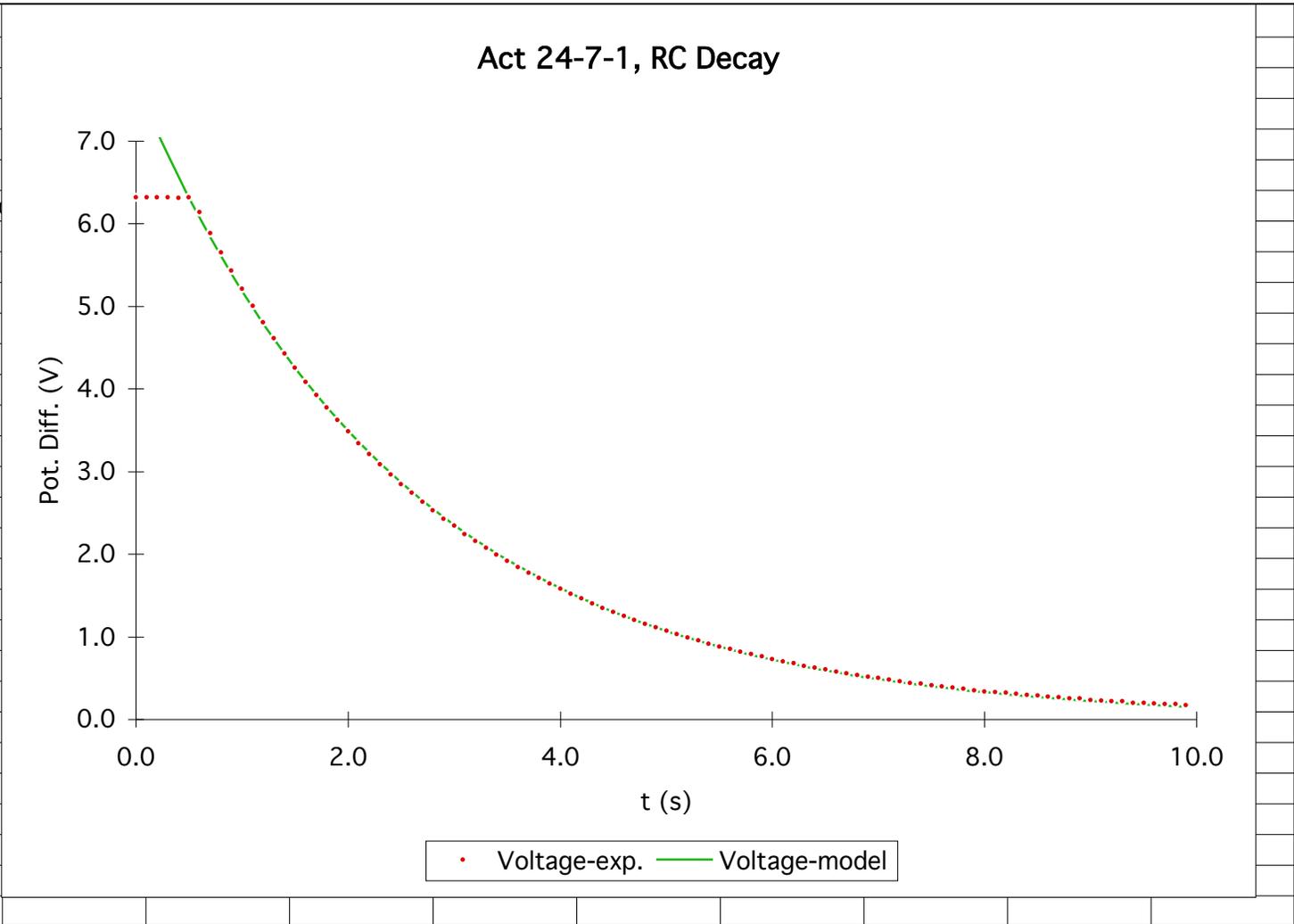
1) “ $RC$  time constant”:  $\tau = RC$ .

2) “*Half-life*,  $t_{1/2}$ ”: the time it takes for  $\Delta V_C$  to decay from  $\Delta V_0$  to  $\Delta V_0/2$ .

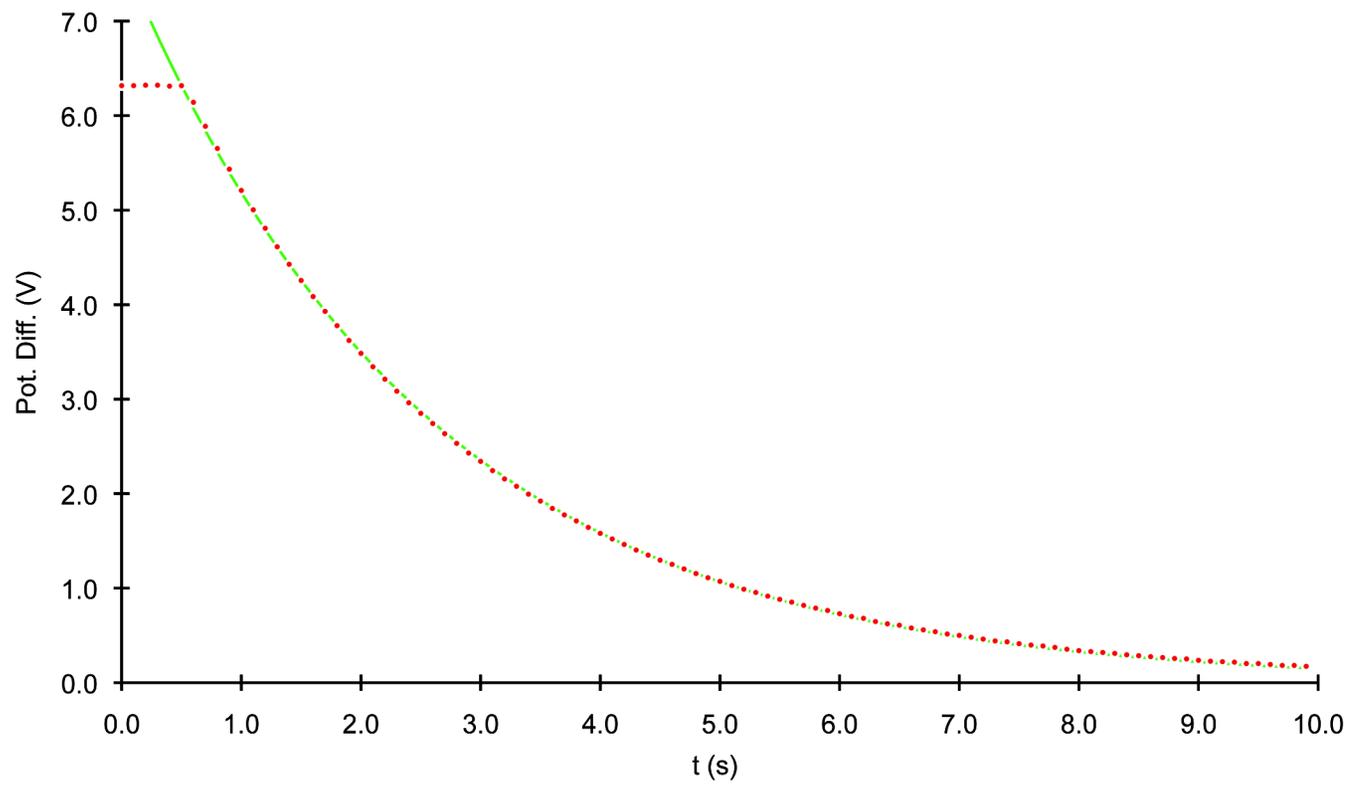
$\Delta V =$	6.34	
$R =$	980	
$C =$	4.56E-03	
<i>Act 24-7-1, RC Decay</i>		
Pot. Diff. (V)		
t (s)	Voltage-exp	Voltage-mo
0.0	6.342	7.091
0.1	6.342	6.934
0.2	6.347	6.781
0.3	6.347	6.631
0.4	6.342	6.484
0.5	6.347	6.340
0.6	6.220	6.200
0.7	6.068	6.062
0.8	5.937	5.928
0.9	5.800	5.797
1.0	5.668	5.668
1.1	5.541	5.543
1.2	5.414	5.420
1.3	5.287	5.300
1.4	5.170	5.182
1.5	5.062	5.068
1.6	4.945	4.955
1.7	4.833	4.846
1.8	4.730	4.738
1.9	4.628	4.633
2.0	4.520	4.531
2.1	4.418	4.430
2.2	4.320	4.332



$\Delta V =$	6.32	
$R =$	1000	
$C =$	2.53E-03	
<i>Act 24-7-1, RC Decay</i>		
Pot. Diff. (V)		
t (s)	Voltage-exp	Voltage-mo
0.0	6.317	7.700
0.1	6.317	7.402
0.2	6.322	7.115
0.3	6.322	6.839
0.4	6.313	6.575
0.5	6.317	6.320
0.6	6.142	6.075
0.7	5.888	5.840
0.8	5.653	5.614
0.9	5.433	5.396
1.0	5.209	5.187
1.1	5.004	4.987
1.2	4.808	4.793
1.3	4.613	4.608
1.4	4.427	4.429
1.5	4.256	4.258
1.6	4.085	4.093
1.7	3.929	3.935
1.8	3.778	3.782
1.9	3.621	3.636
2.0	3.485	3.495
2.1	3.343	3.360
2.2	3.211	3.229

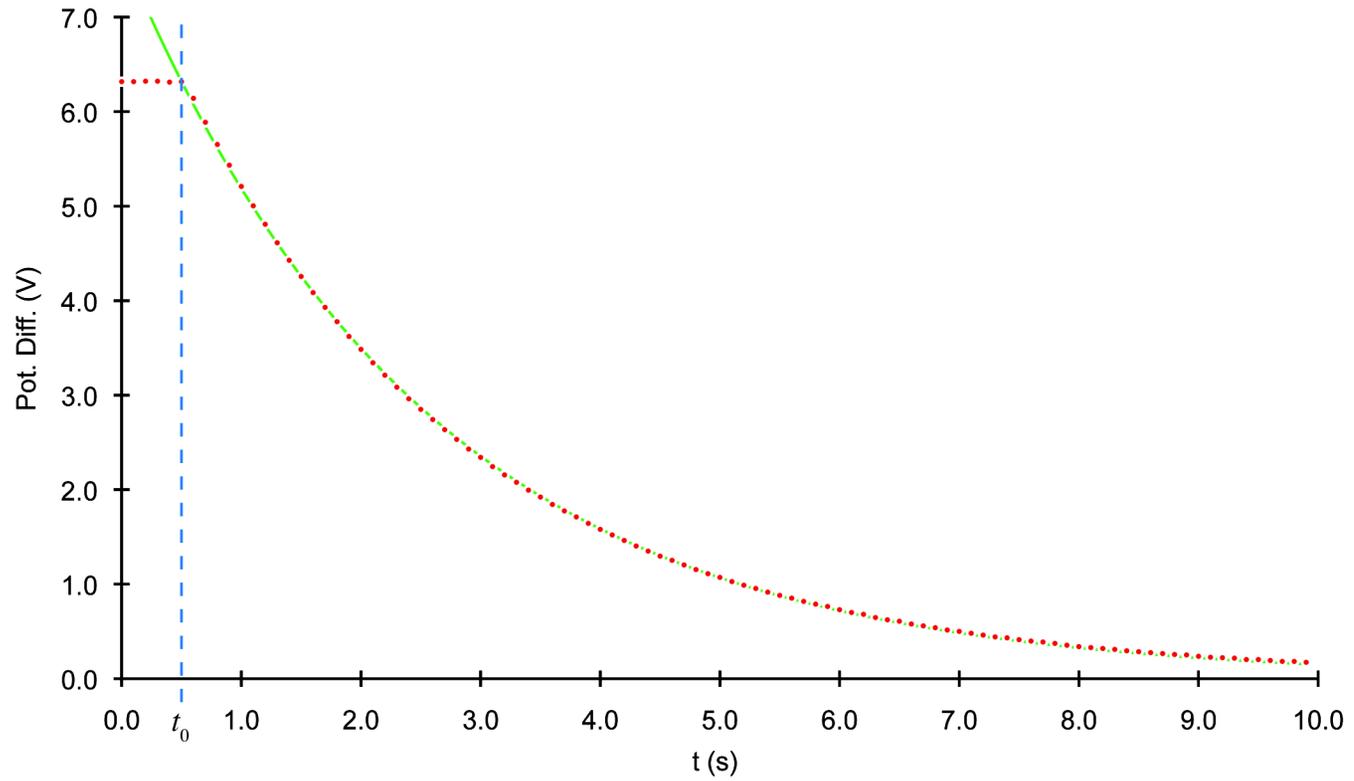


**Act 24-7-1, RC Decay**  
 $R = 1000 \Omega$ ,  $C = 2532 \mu\text{F}$



• Voltage-exp.    — Voltage-model

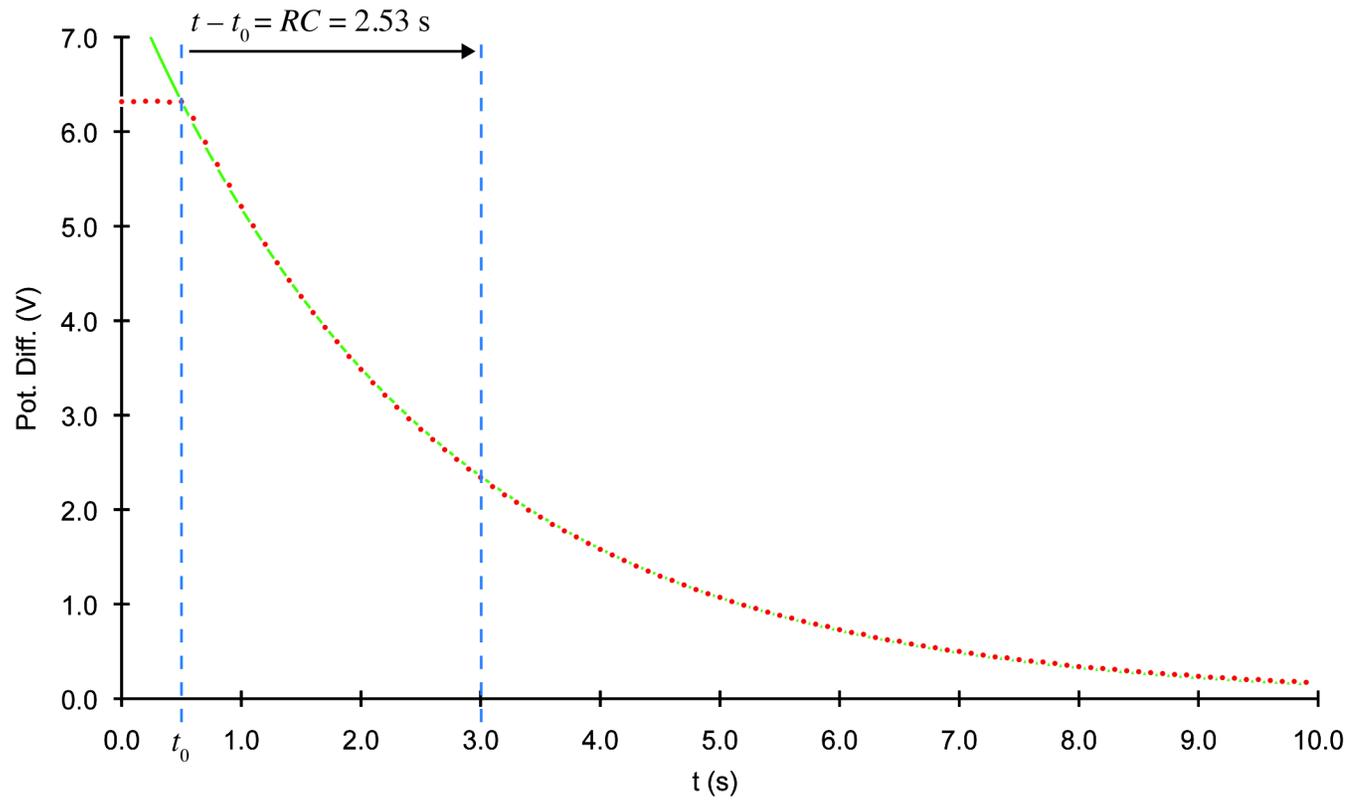
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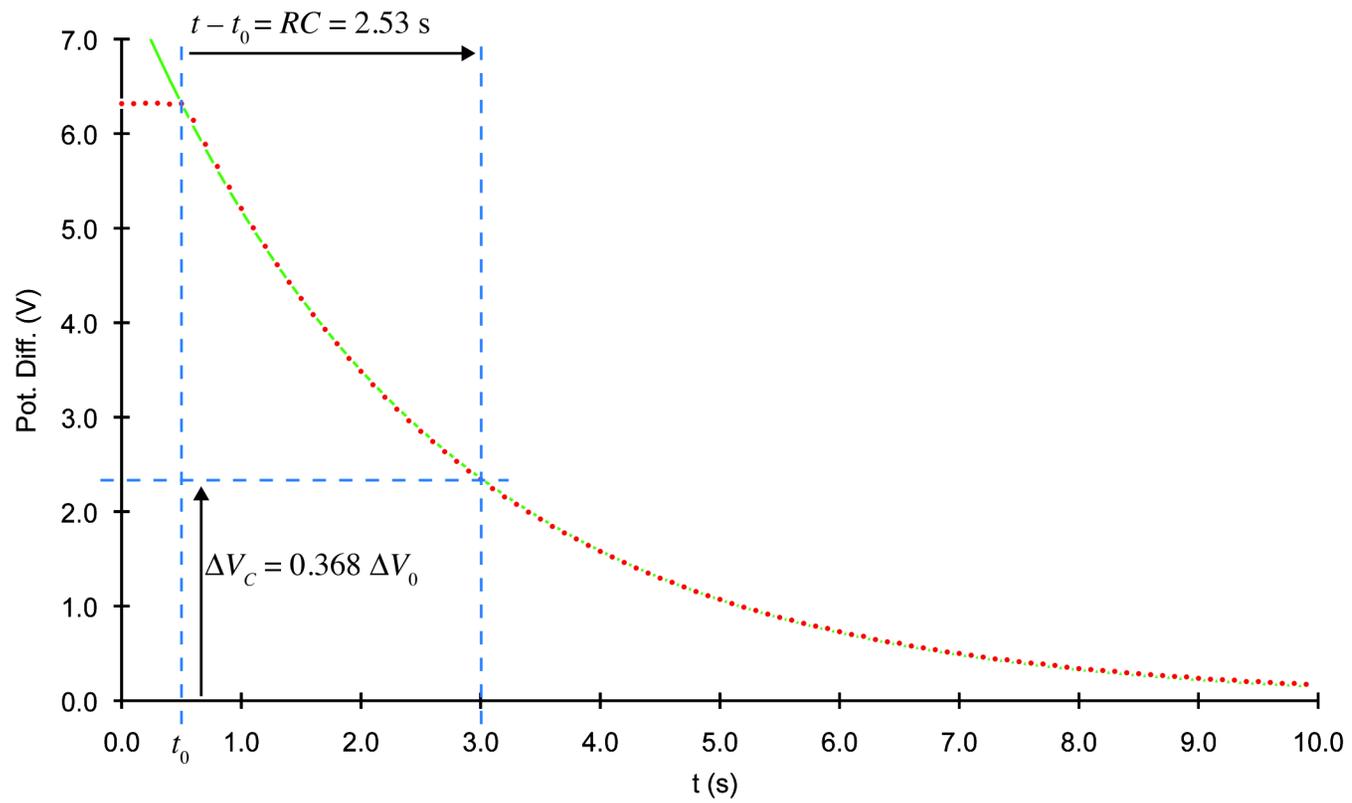
$R = 1000 \Omega$ ,  $C = 2532 \mu\text{F}$



• Voltage-exp.    — Voltage-model

### Act 24-7-1, RC Decay

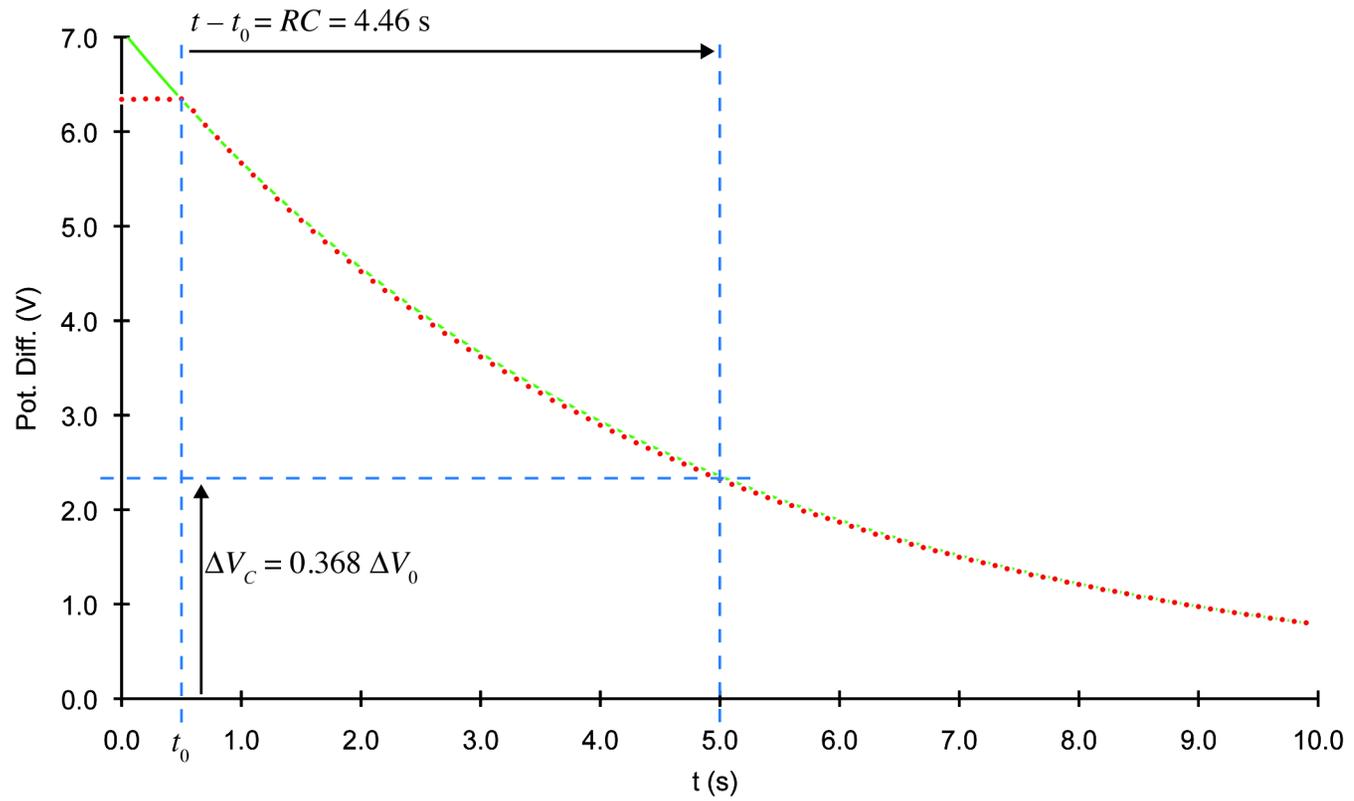
$R = 1000 \Omega$ ,  $C = 2532 \mu\text{F}$



• Voltage-exp. — Voltage-model

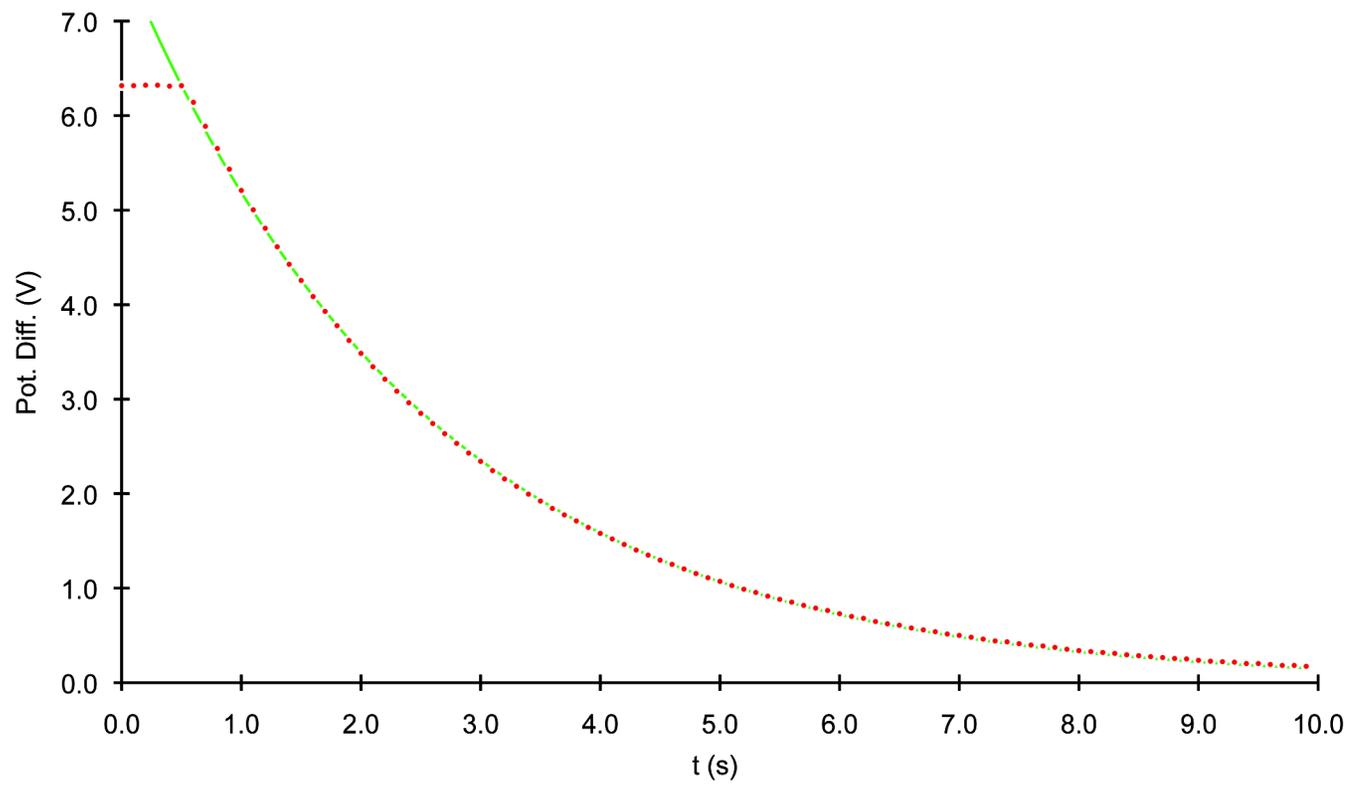
### Act 24-7-1, RC Decay

$R = 980 \Omega$ ,  $C = 4555 \mu\text{F}$



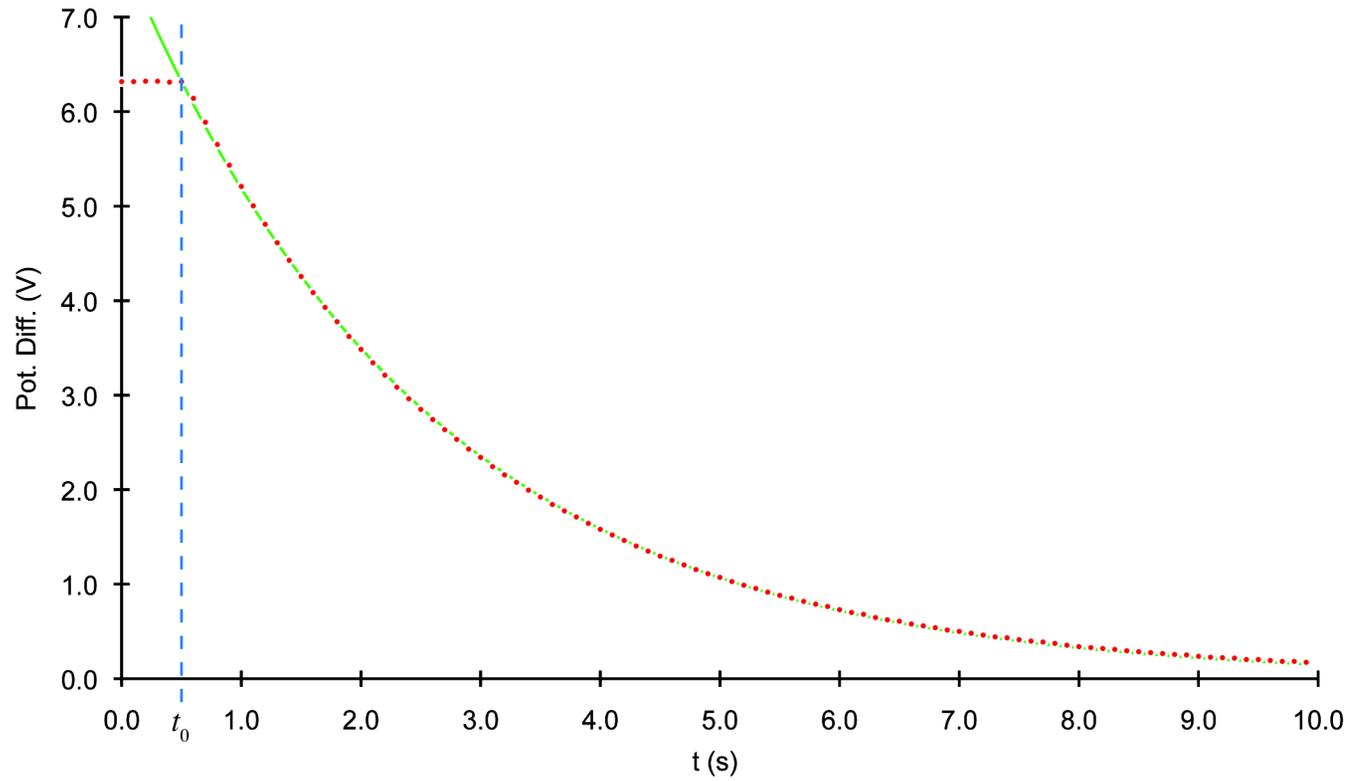
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 $R = 1000 \Omega$ ,  $C = 2532 \mu\text{F}$



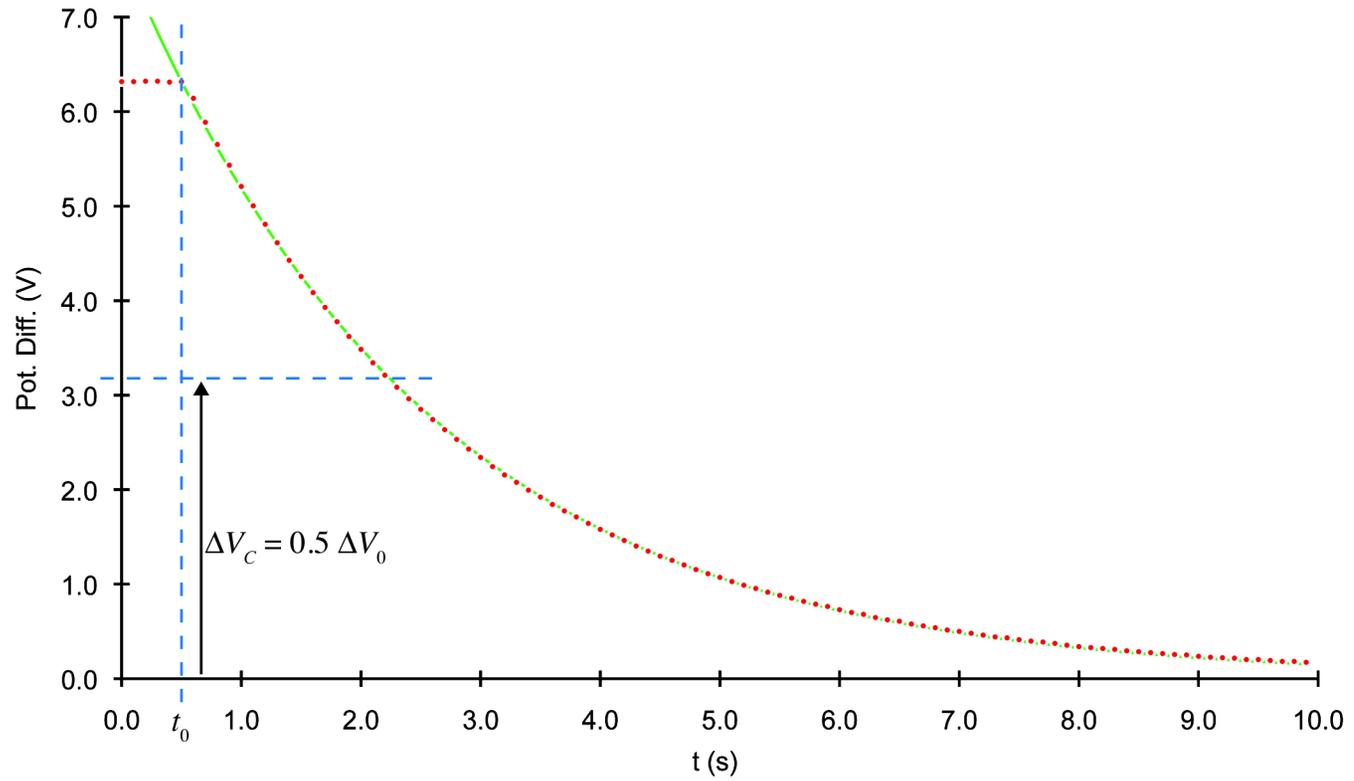
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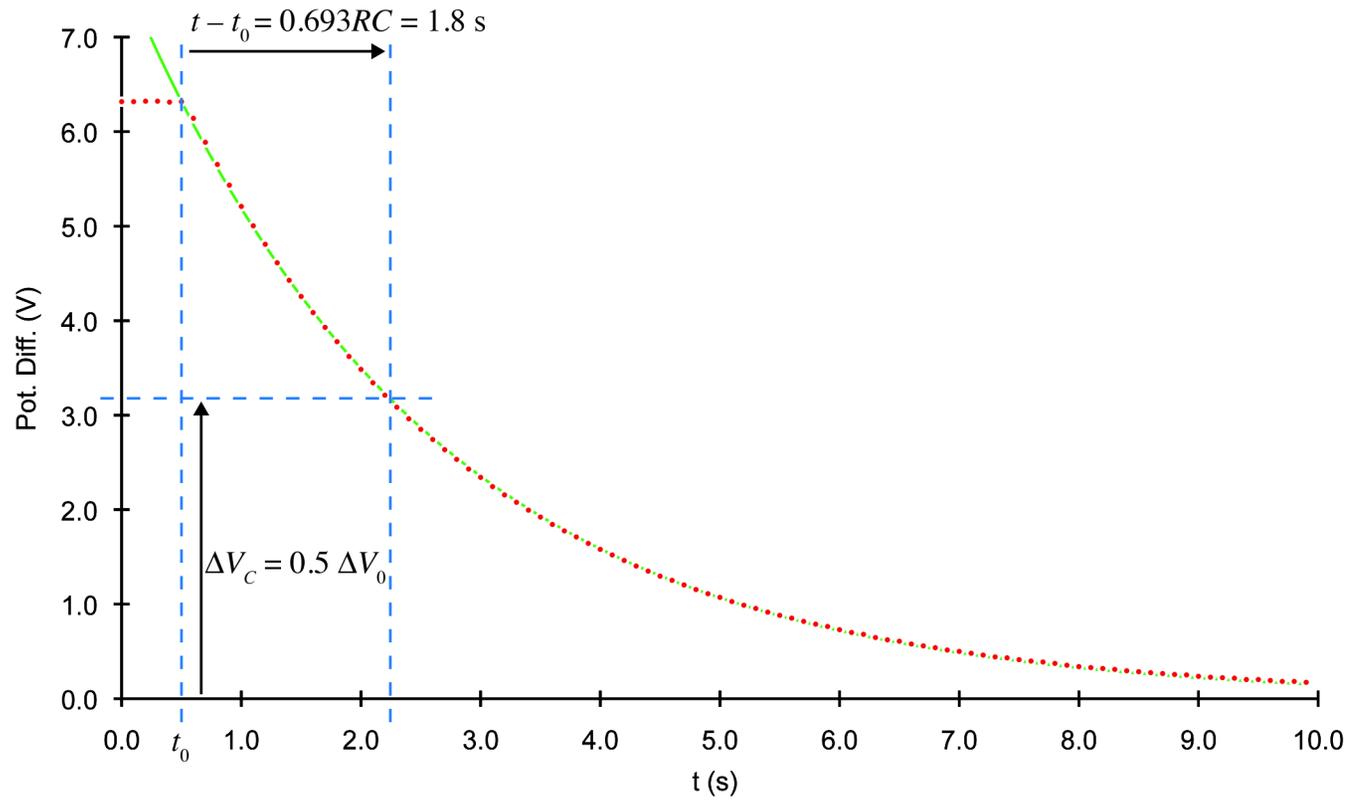
**Act 24-7-1, RC Decay**  
 $R = 1000 \Omega, C = 2532 \mu\text{F}$



• Voltage-exp.    — Voltage-model

### Act 24-7-1, RC Decay

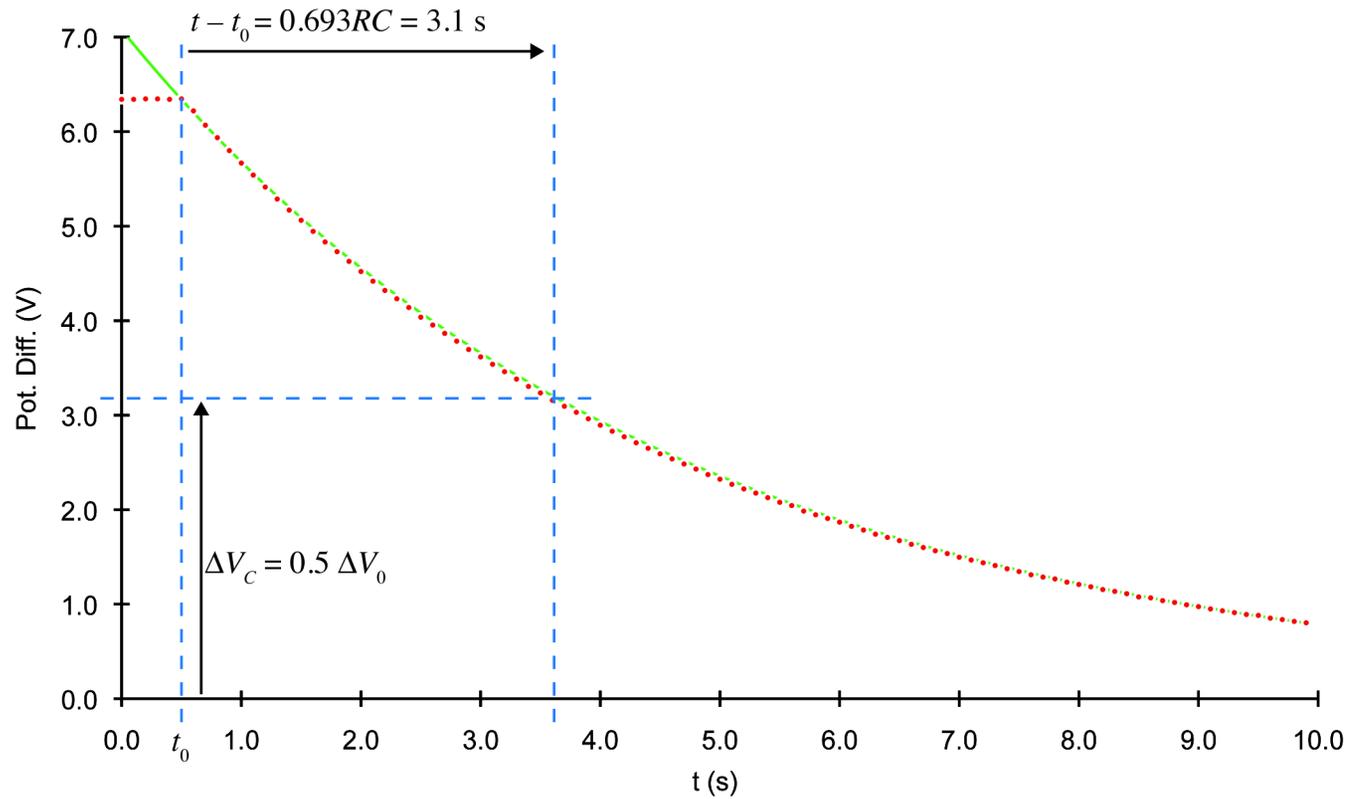
$R = 1000 \Omega$ ,  $C = 2532 \mu\text{F}$



• Voltage-exp.    — Voltage-model

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$R = 980 \Omega$ ,  $C = 4555 \mu\text{F}$



• Voltage-exp.    — Voltage-model